

Erratum: Ground-state factorization and quantum phase transition in dimerized spin chains [Phys. Rev. B **79**, 060405 (2009)]

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There are some formulas that are incorrect.

In the calculation of the factorizing field for the nearest-neighbor Hamiltonian (1), I wrote (page 2, first column) $h_F = [(J_1 + J_2)/2]\sqrt{1 - \gamma^2}$. Actually, the correct version is $h_F = [(J_1 + J_2)/2]\sqrt{1 - \kappa^2}$ (the parameter γ does not exist).

The conditions for the existence of the factorized ground state in the presence of long-range interaction are not correct in the antiferromagnetic scenario. When $(J_{1,i}^x + J_{1,i}^y) > 0$, the scaling conditions as a function of the interaction distance are $J_{r,i}^{x,y} = (-1)^r \gamma_r J_{1,i}^{x,y}$ and $J_{r,i}^z = \gamma_r J_{1,i}^z$. As a consequence, the factorized point amounts to $h_F = (1 + \kappa)\sqrt{(\mathcal{F}_1^x - \mathcal{F}_1^y)(\mathcal{F}_1^x + \mathcal{F}_1^y)}$, with $\mathcal{F}_1^z = \sum_r J_{r,1}^z$ and $\mathcal{F}_1^{x,y} = \sum_r (-1)^r J_{r,1}^{x,y}$.

In the hybrid case, the scaling conditions are correct, while the value of the factorizing field is, as in the other cases, $h_F = (1 + \kappa)\sqrt{(\mathcal{F}_1^x - \mathcal{F}_1^y)(\mathcal{F}_1^x + \mathcal{F}_1^y)}$ (the difference is in the definition of \mathcal{F}_1^z).

In a recent work,¹ Giampaolo and coworkers claimed that it would not be possible to formulate a general theory of ground state factorization without defining a very specific measure (the so-called extremal single-qubit unitary operation), on the basis of an example showing the wrongness of my results. Their counterexample being based on the incorrect formulas I amended here, all the conclusions of the paper are valid.

¹S. M. Giampaolo, G. Adesso, and F. Illuminati, Phys. Rev. B **79**, 224434 (2009).